

Mathematics, Statistics, and Computer Science* MAJORS, MINORS

ASSOCIATE PROFESSORS: Julie M. Clark (on leave Term 1)

ASSISTANT PROFESSOR: Emelie Curl, Molly Lynch (chair), Giancarlo Schrementi

LECTURER: Erin Levering (director of Quantitative Reasoning)

The study of mathematics is motivated by its intrinsic beauty as well as its applicability to everyday life. Mathematics promotes a strengthening of critical and analytical problem-solving skills.

A student graduating with a mathematics major from Hollins will be a logical thinker who is well educated in major areas of mathematics (calculus, linear algebra, statistics, algebra, and analysis), in the application of mathematical concepts to problem solving, and in the development and communication of applied and theoretical mathematics. A recent survey of mathematics majors shows careers as bankers, teachers, defense analysts, actuaries, and programmers and graduate school placements in mathematics, forensic science, medicine, and law.

*Note: Hollins does not offer a major or minor in either statistics or computer science.

REQUIREMENTS FOR A MAJOR IN MATHEMATICS (B.A.):

13 courses (40–42 credits)

- MATH 241: Calculus I (6)
- MATH 242: Calculus II (4)
- MATH 246: Laboratories in Mathematical Experimentation (2)
- MATH 255: Methods of Matrices and Linear Algebra (4)
- MATH 310: A Transition to Advanced Mathematics (4)
- MATH 316: Several-Variable Calculus (4)
- A 300-level MATH course in algebra (2) (Alg)
- A 300-level MATH course in analysis (2) (Ana)
- At least two additional 300-level MATH, STAT or CMPS 2 credit courses (4)
- MATH 471: Senior Seminar (2)
- MATH 490 (2, 2) or MATH 480 (2 and Short Term) or MATH 472 (2) as determined in consultation with members of the department
- STAT 251: Statistical Methods (4)

A student is exempted from MATH 241 and MATH 242 if she can demonstrate to the department's satisfaction her knowledge of the course(s).

REQUIREMENTS FOR A MAJOR IN MATHEMATICS (B.S.):

19 courses (64–70 credits)

REQUIRED COURSES IN MATHEMATICS AND STATISTICS:

- MATH 241: Calculus I (6)
- MATH 242: Calculus II (4)
- MATH 246: Laboratories in Mathematical Experimentation (2)
- MATH 255: Methods of Matrices and Linear Algebra (4)
- MATH 310: A Transition to Advanced Mathematics (4)
- MATH 316: Several-Variable Calculus (4)
- A 300-level MATH course in algebra (2) (Alg)
- A 300-level MATH course in analysis (2) (Ana)
- At least four additional 300-level MATH, STAT or CMPS 2 credit courses (8)
- MATH 471: Senior Seminar (2)
- MATH 490 (2, 2) or MATH 480 (2 and Short Term) or MATH 472 (2) as determined in consultation with members of the department
- STAT 251: Statistical Methods (4)

A student may be exempted from MATH 241 and MATH 242 if she can demonstrate to the department's satisfaction her knowledge of the course(s).

REQUIRED ALLIED COURSES:

- Two courses (with laboratories) above the 200 level* from at least two of the following departments: biology, chemistry, computer science, or physics, or four courses (with laboratories) above the 200 level* from the departments of biology, chemistry, or physics
- * or CHEM 105/105L: Principles of Chemistry or CMPS 160: Applied Computing I with Python; note that for the purposes of this requirement, a 4-credit CMPS course is considered to be a course with lab

REQUIREMENTS FOR A MAJOR IN MATHEMATICS WITH A DATA SCIENCE CONCENTRATION (B.S.):

19 courses (62-68 credits)

- MATH 241: Calculus I (6)
- MATH 242: Calculus II (4)
- MATH 246: Laboratories in Mathematical Experimentation (2)
- MATH 255: Methods of Matrices and Linear Algebra (4)
- MATH 310: A Transition to Advanced Mathematics (4)
- MATH 316: Several-Variable Calculus (4)
- A 300-level MATH course in algebra (2) (Alg)
- A 300-level MATH course in analysis (2) (Ana)
- At least two additional 200- or 300-level MATH, STAT or CMPS 2-4 credit courses (4-8)
- MATH 471: Senior Seminar (2)
- MATH 490 (2, 2) or MATH 480 (2 and Short Term) or MATH 472 (2) as determined in consultation with members of the department
- STAT 251: Statistical Methods (4)

REQUIRED ALLIED COURSE:

- One course with laboratory at or above the 200-level from one of the following departments: biology, chemistry, or physics.

REQUIRED COURSES IN COMPUTER SCIENCE:

- CMPS 160: Applied Computing I with Python (4)
- CMPS 217: Data Structures (4)
- CMPS 260 Applied Computing II: How to Think Like a Data Scientist (4)
- CMPS 335: Data Mining Techniques (2)

A student may be exempted from MATH 241 and MATH 242 if she can demonstrate to the department's satisfaction her knowledge of the course(s).

REQUIREMENTS FOR A MINOR IN MATHEMATICS:

5 courses (20 credits)

- MATH 241: Calculus I (6)
- MATH 242: Calculus II (4)
- MATH 246: Laboratories in Mathematical Experimentation (2)
- MATH 255: Methods of Matrices and Linear Algebra (4) **or** STAT 251: Statistical Methods (4)
- MATH 310: A Transition to Advanced Mathematics (4)

REQUIREMENTS FOR A MINOR IN DATA SCIENCE:

7 courses (22 credits)

- STAT 251: Statistical Methods I (4)
- STAT 324: Data Wrangling (2)
- CMPS 160: Applied Computing I with Python (4)
- CMPS 217: Data Structures (4)
- CMPS 260 Applied Computing II: How to Think Like a Data Scientist (4)
- CMPS 335: Data Mining Techniques (2)
- Two elective credits in STAT or CMPS at the 300 level

PLACEMENT IN MATHEMATICS AND STATISTICS COURSES:

A diagnostic/placement examination is recommended as a prerequisite for initial enrollment in any one of the following courses: MATH 130, MATH 140, MATH 152, MATH 241, STAT 140, and STAT 251.

COURSES IN MATHEMATICS:

MATH 100: INTRODUCTION TO QUANTITATIVE REASONING (4)

Levering

This course is for students who need practice in applying fundamental mathematical skills (algebra, graphing, geometry, data analysis, and linearity) to real-life applications. The goal of the course is to develop the quantitative skills that promote problem solving with confidence. Prerequisite: appropriate score on Math/QR assessment. Offered both terms. (q)

MATH 105: QUANTITATIVE REASONING IN TODAY'S WORLD (4)

Curl, Lynch, Schrementi

This course focuses on the application of mathematics to the students' personal and social issues. It is designed to prepare students for the mathematics they will encounter in other college classes, particularly in the social and natural sciences such as problem solving, financial management, and growth. The course provides students with critical thinking and quantitative reasoning skills needed to understand major issues in life. It develops students' ability to reason with quantitative information necessary to achieve success in a career. Prerequisite: appropriate score on Math/QR assessment. Offered both terms. (q)

MATH 130: MATHEMATICAL MODELING WITH PRECALCULUS (4)

Lynch

Emphasis is on the application of algebra, precalculus, and mathematical models to many exciting real-world problems in art, music, business, economics, statistics, and biology and other sciences. Recommended for prospective teachers and non-mathematicians. Prerequisite: appropriate score on Math/QR assessment. Offered both terms. (q)

MATH 140: PRECALCULUS (4)

Levering

A study of precalculus involving the application of functions and mathematical models to real-world problems in the natural sciences as well as art, music, business, economics, and the social sciences. Provides a minimal preparation for the calculus sequence. Recommended for prospective teachers. Prerequisites: q. Offered Term 2. (Q)

MATH 152: INTUITIVE CALCULUS (4)

Department

Ideas and techniques of the one-variable calculus required to solve problems in a variety of disciplines. Concepts are presented from a geometric or intuitive point of view. Prerequisites: q and MATH 140 (or higher), or MATH 105 and permission, or equivalent. Not offered in 2023-24. (Q)

MATH 211: SYMBOLIC LOGIC (4)

Downey

Also listed and described as PHIL 211. Open to first-year students with permission. Prerequisite: q. Offered Term 1. (Q)

MATH 241, 242: CALCULUS I, II (6, 4)

Lynch, Curl

The calculus of real functions of one real variable with emphasis on application of concepts to real world problems. Calculus I: functions, limits, continuity, the derivative, and applications of the derivative. Calculus II: antiderivatives, integrals, applications of the integral, improper integrals, sequences, and series. Open to first-year students. Prerequisites: for MATH 241: q and MATH 140 or equivalent; for MATH 242: MATH 241. MATH 241 meets daily. Offered consecutive terms. (Q)

MATH 246: LABORATORIES IN MATHEMATICAL EXPERIMENTATION (2)

Clark

A course in mathematical discovery. Students "do" mathematics by designing mathematical experiments, obtaining mathematical results, analyzing data, and making mathematical conjectures. Topics include fractals, cryptography, function iteration and chaos, strategy of games, and graph theory. Prerequisite: MATH 241. Open to first-year students. Offered Term 2.

MATH 255: METHODS OF MATRICES AND LINEAR ALGEBRA (4)

Lynch

Properties of matrices; methods of finding an inverse; matrix equations and solutions; characteristic roots, important matrix forms; applications in social and physical sciences. Prerequisites: q and one college mathematics course above MATH 140 and permission. Open to first-year students. Not offered in 2023-24. (Q)

MATH 290: INDEPENDENT STUDY (2 or 4)**Department**

Independent study conducted below the advanced level. Application must be made with faculty prior to registration. Offered any term.

MATH 310: A TRANSITION TO ADVANCED MATHEMATICS (4)**Curl**

An introduction to the standard methods of mathematical proof and their validity. Methods of proof are examined in detail, and examples of each method are analyzed carefully. The emphasis is on enhancing students' ability to write and understand mathematical proofs. Prerequisite: MATH 242 or permission. Offered Term 1.

MATH 316: SEVERAL-VARIABLE CALCULUS (4)**Curl**

The calculus of functions of several real variables: vector spaces; differentiation of vector functions; partial derivatives; maxima and minima; and multiple integrals. Prerequisites: MATH 242. Offered Term 1.

MATH 343: COMBINATORICS (2)**Lynch**

An introduction to combinatorics, with potential topics including basic counting principles, recursions, permutations, graph theory, and partially ordered sets. Prerequisite: MATH 242 or equivalent. Not offered in 2023-24.

MATH 351: DIFFERENTIAL EQUATIONS (2)**Curl**

An introduction to ordinary differential equations with an emphasis on applications. The course topics include first order differential equations, separable equations, linear second order differential equations, the Laplace Transform, series solutions, and numerical methods. Prerequisite: Math 242 or equivalent. (Gen) Offered Term 2.

MATH 352: FIELDS AND CODES (2)**Clark**

An introduction to algebraic coding theory using finite fields and number-theory. Codes studied include binary, hexadecimal, ASCII, the error-correcting Hamming codes, BHC, and Reed-Solomon codes. Prerequisite: MATH 242 or equivalent. (Alg) Offered Term 2.

MATH 360: ANALYSIS: ITERATIONS AND DYNAMICAL SYSTEMS (2)**Clark**

A mathematical study of convergence and limits. Students actively investigate concepts using numerical techniques followed by precise and careful analysis. Topics include fractals, linear and non-linear function iteration, basins of attraction, chaos, complex numbers, and Newton's method. (Ana) Not offered in 2023-24.

MATH 361: COMPLEX VARIABLES (2)**Lynch**

An introduction to complex analysis, with topics including the algebra of complex numbers, analytic functions, elementary functions, contour integrals, and Laurent series. (Ana) Prerequisite: Math 242 or equivalent. Not offered in 2023-24.

MATH 362: REAL ANALYSIS (2)**Department**

An introduction to advanced calculus. Students will be reading and writing mathematical proofs that provide the theoretical basis for important topics from single-variable calculus, including limits, continuity, differentiation, integration, sequences, and series. (Ana) Prerequisite: Math 242 and MATH 310. Not offered in 2023-24.

MATH 390: INDEPENDENT STUDY (2 or 4)**Department**

Independent study conducted at the advanced level. Application must be made with faculty prior to registration. Offered any term.

MATH 397: TEACHING MATHEMATICS IN THE ELEMENTARY AND MIDDLE SCHOOLS (4) Levering

This course will address content knowledge, curriculum development, methodologies, assessment and evaluation, using resources and technology, and approaches to teaching elementary and middle school mathematics, within the framework of the NCTM Standards of Learning, the VA Standards of Learning, and VA Early Learning and Development Standards. Attention will be given to problems that students have in learning and understanding mathematics and ways to address those problems. Prerequisite: *q*. Offered Term 1.

MATH 399: INTERNSHIP (2 or 4)**Department**

Application must be made with faculty prior to registration. May be proposed in any term.

MATH 471: SENIOR SEMINAR (2)**Lynch**

Emphasis is on written and oral communication of mathematical ideas. Senior mathematics majors complete a mathematics portfolio based on select assignments from previous mathematics, computer science, and statistics courses. Prerequisite: senior standing. Offered Term 1.

MATH 472: SENIOR SEMINAR (2)**Curl**

In this course students have an opportunity to explore advanced and/or new mathematical topics. Students may suggest projects to departmental faculty for their approval and guidance. Students will present completed projects at the end of the semester. Offered Term 2.

MATH 480: SENIOR THESIS (2)**Department**

An extensive research project to be carried out over one semester and Short Term. Open to qualified senior mathematics majors. Prerequisite: MATH 471. Offered Term 2.

MATH 490: SENIOR HONORS (2, 2)**Department**

Open to majors with permission. Required both regular terms and Short Term. Interested majors should consult with the chair of the department no later than the end of the second term of their junior year. Application must be made with faculty prior to registration.

COURSES IN STATISTICS:**STAT 140: INTRODUCTION TO STATISTICS (4)****Clark, Lynch**

Topics are methods of description, measures of location and dispersion, simple linear regression, normal distributions, sampling distributions, interval estimation, and significance tests of proportions. Applications in both physical and social sciences. Prerequisite: q. Offered Term 2. (Q)

STAT 251: STATISTICAL METHODS (4)**Clark**

Statistical inference for surveys and controlled experiments. Use of a statistical computer package required. Measures of central tendency and dispersion, normal, binomial, and t-distributions; Fisher's exact test, sampling distributions; estimation and significance testing; analysis of variance; linear regression and correlation and commonly used transformations. Prerequisite: q and appropriate recommendation from Math/QR assessment. Offered Term 2. (Q)

STAT 324: DATA WRANGLING WITH R (2)**Clark**

An introduction to skills necessary for data wrangling and other modern techniques of statistical interpretation. Students will learn and practice techniques for acquiring, tidying, mutating, and merging data and data visualization, using R-Studio and the RMarkdown document writing system. Pre-requisite: q. Offered Term 2.

STAT 343: PROBABILITY (2)**Clark**

An introduction to combinatorial analysis, the axioms of probability, conditional probability, independence, discrete and continuous random variables, expectation and moment generating functions and stochastic processes. Students will actively investigate probabilistic situations and perform simulations. Open to first-year students. Prerequisite: Math 242. Offered by request in 2023-24.

STAT 361: REGRESSION (2)**Clark**

The analysis of continuous response data. The focus is on linear and multiple regression with theoretical and practical training in statistical modeling. This is a hands-on, applied course where students will become proficient using R-Studio and Minitab to analyze data from a variety of fields and will learn what assumptions underlie their models, how to test whether the data meet the assumptions, and what can be done when the assumptions are not met. Prerequisites: STAT 140 or STAT 251, or equivalent. Not offered in 2023-24.

COURSES IN COMPUTER SCIENCE:**CMPS 110: COMPUTER BASICS AND APPLICATIONS (2)****Schrementi**

An introduction to the basics of personal computers and applications using Microsoft Office, including word processing, spreadsheets, presentations, email, and database management. Course is offered online and requires students to work independently. Offered both terms.

CMPS 160: APPLIED COMPUTING I WITH PYTHON (4)**Schrementi**

This introduction to computer science, developed by Google and their university partners, emphasizes problem solving and data analysis skills along with computer programming skills. Using Python, students will learn design, implementation, testing, and analysis of algorithms and programs. Within the context of programming, students will learn to formulate problems, think creatively about solutions, and express those solutions clearly and accurately.

Problems will be chosen from real-world examples such as graphics, image processing, cryptography, data analysis, and video games. Prerequisite: *q*. Offered Term 1. (Q)

CMPS 217: DATA STRUCTURES (4)

Schrementi

Students will study fundamental data structures and their applications to problem solving. Object-oriented programming (OOP) is introduced, and OOP techniques are explored, including inheritance, polymorphism, interfaces, and abstract classes. Software engineering concepts of design principles and testing methods are also covered. Prerequisite: CMPS 160 or permission. Offered Term 2.

CMPS 260: APPLIED COMPUTING II: HOW TO THINK LIKE A DATA SCIENTIST (4)

Schrementi

Introduces students to the importance of gathering, cleaning, normalizing, visualizing and analyzing data to drive informed decision-making, no matter the field of study. Real-world datasets will be analyzed using a combination of tools and techniques, including spreadsheets, Python, and SQL. Students will learn to ask good, exploratory questions and develop metrics for designing a well-thought-out analysis. Presenting and discussing an analysis of datasets will be an important component of the course. Prerequisite CMPS 160. Offered Term 2.

CMPS 290: INDEPENDENT STUDY (2 or 4)

Department

Independent study conducted below the advanced level. Application must be made with faculty prior to registration. Offered any term.

CMPS 325: MACHINE LEARNING (2)

Schrementi

An introduction to machine learning with a focus on understanding the fundamentals of neural network learning. Topics include Hebbian learning, single and multi-layer perceptrons, and data preparation techniques for improving learning. Open to first-year students. Prerequisite: MATH 241 or permission. Offered Term 2.

CMPS 335: DATA MINING TECHNIQUES (2)

Schrementi

Students will study supervised and unsupervised strategies for data analysis and predictive modeling, including decision trees, clustering, and association rule learning. Prerequisite/Corequisite: MATH 241 or permission. Offered Term 1.